

Enrollment No: _____

Exam Seat No: _____

C. U. SHAH UNIVERSITY

Winter Examination-2019

Subject Name : Engineering Mathematics – 3

Subject Code : 4TE03EMT2

Branch: B. Tech (All)

Semester : 3

Date : 13/11/2019

Time : 02:30 To 05:30

Marks : 70

Instructions:

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

Q-1 Attempt the following questions: (14)

- a) If $f(x) = x$ is represented by Fourier series in $(-\pi, \pi)$ then a_0 equal to
(A) $\frac{\pi}{2}$ (B) π (C) 0 (D) 2π
- b) If $f(x) = x^2$ is represented by Fourier series in $(-\pi, \pi)$ then b_n equal to
(A) $\frac{\pi^2}{3}$ (B) 0 (C) $\frac{2\pi^2}{3}$ (D) $\frac{\pi^2}{6}$
- c) Fourier expansion of an even function $f(x)$ in $(-\pi, \pi)$ has
(A) only sine terms (B) only cosine terms
(C) both sine and cosine terms (D) None of these
- d) Inverse Laplace transform of $\frac{1}{(s+4)^6}$ is
(A) $e^{-6t} \frac{t^4}{4!}$ (B) $e^{-4t} \frac{t^6}{6!}$ (C) $e^{-4t} \frac{t^5}{5!}$ (D) $e^{-4t} \frac{t^6}{5!}$
- e) Laplace transform of C^{t+1} is
(A) $\frac{1}{s-c}$ (B) $\frac{c}{s-\log c}$ ($s > \log c$) (C) $\frac{c^2}{s+\log c}$ (D) none of these
- f) Laplace transform of $t \sin at$ is
(A) $\frac{2as}{(s^2+a^2)^2}$ (B) $\frac{as}{(s^2+a^2)^2}$ (C) $\frac{2s}{(s^2+a^2)^2}$ (D) $\frac{2as}{s^2+a^2}$
- g) The C. F. of the differential equation $(D^2 + 3D + 2)y = e^{2x}$ is
(A) $c_1e^x + c_2e^{2x}$ (B) $c_1e^{-x} + c_2e^{-2x}$ (C) $c_1e^{-x} + c_2e^{2x}$ (D) $c_1e^x + c_2e^{-2x}$
- h) The P. I. of $(D^2 - 4)y = 2^x$ is



- (A) $\frac{2^x}{(\log 2)^2 + 4}$ (B) $\frac{2^x}{(\log 2)^2 - 4}$ (C) $\frac{2^x}{\log 2 - 4}$ (D) none of these
- i) The P. I. of $(D^2 + a^2)y = \sin ax$ is
 (A) $-\frac{x}{2a} \cos ax$ (B) $\frac{x}{2a} \cos ax$ (C) $-\frac{ax}{2} \cos ax$ (D) $\frac{ax}{2} \cos ax$
- j) Eliminating the arbitrary constants, a and b from $x^2 + y^2 + (z - c)^2 = a^2$, the partial differential equation formed is
 (A) $xp = yq$ (B) $xq = yp$ (C) $z = pq$ (D) None of these
- k) The general solution of the equation $(y - z)p + (z - x)q = x - y$ is
 (A) $F(x^2 + y^2 + z^2, x + y + z) = 0$ (B) $F(xyz, x^2 + y^2 + z^2) = 0$
 (C) $F(xy, x^2 + y^2 + z^2) = 0$ (D) none of these
- l) Particular integral of $(2D^2 - 3DD' + D'^2)z = e^{x+2y}$ is
 (A) xe^{x+2y} (B) $\frac{1}{2}e^{x+2y}$ (C) $-\frac{x}{2}e^{x+2y}$ (D) $\frac{x^2}{2}e^{x+2y}$
- m) Iterative formula for finding the square root of N by Newton-Raphson method is
 (A) $x_{i+1} = \frac{1}{2} \left(x_i - \frac{N}{x_i} \right)$ ($i = 0, 1, 2, \dots$) (B) $x_{i+1} = \frac{1}{2} \left(x_i + \frac{N}{x_i} \right)$ ($i = 0, 1, 2, \dots$)
 (C) $x_{i+1} = x_i(2 - Nx_i)$ ($i = 0, 1, 2, \dots$) (D) none of these
- n) The interval $[a, b]$ on which fixed point iteration will converge for the equation $x = \frac{5}{x^2} + 2$ is
 (A) $[2.5, 3]$ (B) $[2, 2.1]$ (C) $[2, 3]$ (D) none of these

Attempt any four questions from Q-2 to Q-8

- Q-2** **Attempt all questions** (14)
 a) Perform the five iteration of the Bisection method to obtain a root of the equation $f(x) = \cos x - xe^x$. (5)
 b) Compute the real root of $x \log_{10} x - 1.2 = 0$ correct to four decimal places using False position method. (5)
 c) Find the Laplace transform of $f(t)$ defined as $f(t) = \begin{cases} t & , 0 < t < 4 \\ 5 & , t > 4 \end{cases}$. (4)
- Q-3** **Attempt all questions** (14)
 a) Express $f(x) = \frac{1}{4}(\pi - x)^2$ as a Fourier series with period 2π to be valid in the interval 0 to 2π . (5)
 b) Obtain Fourier series for the function $f(x) = \begin{cases} \pi x, & 0 \leq x \leq 1 \\ \pi(2-x), & 1 \leq x \leq 2 \end{cases}$ (5)



- c) Evaluate $\sqrt{5}$ correct to three decimal places using Newton-Raphson method. (4)

Q-4 **Attempt all questions** (14)

- a) Using Laplace transform method solve: (5)

$$y'' + 3y' + 2y = e^t, \quad y(0) = 1, \quad y'(0) = 0$$

- b) Using convolution theorem, evaluate $L^{-1} \left\{ \frac{s}{(s^2 + a^2)^2} \right\}$. (5)

- c) Solve: $\frac{\partial^2 z}{\partial x \partial y} = x^3 + y^3$ (4)

Q-5 **Attempt all questions** (14)

- a) Evaluate: $L^{-1} \left[\frac{s+2}{(s+3)(s+1)^3} \right]$ (5)

- b) Solve: $(D^2 - 4D + 3)y = \sin 3x \cos 2x$ (5)

- c) Solve: $x^2(y-z)p + y^2(z-x)q = z^2(x-y)$ (4)

Q-6 **Attempt all questions** (14)

- a) Solve: $(D^2 + 5D + 4)y = x^2 + 7x + 9$ (5)

- b) If $f(x) = x, \quad 0 < x < \frac{\pi}{2}$ (5)

$$= \pi - x, \quad \frac{\pi}{2} < x < \pi$$

then show that $f(x) = \frac{\pi}{4} - \frac{2}{\pi} \left(\frac{\cos 2x}{1^2} + \frac{\cos 6x}{3^2} + \frac{\cos 10x}{5^2} + \dots \right)$.

- c) Solve: $L \left(\frac{\cos 2t - \cos 3t}{t} \right)$ (4)

Q-7 **Attempt all questions** (14)

- a) Using the method of variation of parameters, (5)

$$\text{Solve: } y'' + 4y' + 4y = \frac{e^{-2x}}{x^2}$$

- b) Solve: $(2x+3)^2 \frac{d^2 y}{dx^2} - 2(2x+3) \frac{dy}{dx} - 12y = 6x$ (5)

- c) Solve: $\frac{\partial^2 z}{\partial x^2} + 3 \frac{\partial^2 z}{\partial x \partial y} + 2 \frac{\partial^2 z}{\partial y^2} = x + y$ (4)

Q-8 **Attempt all questions** (14)

- a) Solve by the method of separation of variables (7)

$$4 \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 3u, \text{ given that } u = 3e^{-y} - e^{-5y} \text{ when } x = 0.$$

- b) Determine the Fourier series up to and including the second harmonic to represent the periodic function $y = f(x)$ defined by the table of values given below. $f(x) = f(x + 2\pi)$ (7)

x°	0	30	60	90	120	150	180	210	240	270	300	330
$f(x)$	0.5	0.8	1.4	2.0	1.9	1.4	1.2	1.4	1.1	0.5	0.3	0.4

